



# Ginzburg-Landau Vortices

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Book Condition: New. Publisher/Verlag: Springer, Basel | The original motivation of this study comes from the following questions that were mentioned to one of us by H. Matano. Let  $G = B = \mathbb{R}^2$ . 1. Consider the Ginzburg-Landau functional  $E_\varepsilon(u) = \int_G |\nabla u|^2 + \frac{1}{4\varepsilon^2} \int_G (|u|^2 - 1)^2$  which is defined for maps  $u \in H^1(G; \mathbb{C})$  also identified with  $H^1(G; \mathbb{R}^2)$ . Fix the boundary condition  $u|_{\partial G} = \gamma$  on  $\partial G$  and set  $H_\varepsilon = \{u \in H^1(G; \mathbb{C}) : u|_{\partial G} = \gamma\}$ . It is easy to see that (2) is achieved by some  $u_\varepsilon$  that is smooth and satisfies the Euler equation in  $G$ ,  $-\Delta u_\varepsilon = \frac{1}{2\varepsilon^2} (|u_\varepsilon|^2 - 1)u_\varepsilon$ . (3)  $\{u_\varepsilon\}$  on  $aG$   $u_\varepsilon \rightarrow u$  The maximum principle easily implies (see e.g., F. Bethuel, H. Brezis and F. Hélein (2)) that any solution  $u_\varepsilon$  of (3) satisfies  $|u_\varepsilon| \sim 1$  in  $G$ . In particular, a subsequence  $(u_{\varepsilon_j})$  converges in the  $W^{1,2}(G)$  topology to a limit  $u$ . | I. Energy estimates for  $S^1$ -valued maps.- 1. An auxiliary linear problem.- 2. Variants of Theorem I.1.- 3.  $S^1$ -valued harmonic maps with prescribed isolated singularities. The canonical harmonic map.- 4. Shrinking holes. Renormalized energy.- II. A lower bound for the energy of  $S^1$ -valued maps on perforated domains.- III. Some basic estimates...



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